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## VIABILITY ANALYSIS FOR A STOCK-CAPITAL FISHERY MODEL

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This work is based on C. Clark, F.Clarke and G. Munro fishery model, [1], where the dynamic is the evolution of both stock and capital controlled by the investment and the part of the capital dedicated to the harvest. The contribution consists of substituting the profit maximization objective by constraints on the states of the model. In this new formulation, we give conditions on the parameters of the model which guarantees the non-emptiness of the viability kernel, which means the determination of the biggest set of initial conditions on which investment and exploitation sustainable policies could be defined. At the center of this result, we find the viability theory introduced by Aubin [3], which consists of studying the existence of controls yielding admissible states. Thus, we build the viability kernel corresponding to the studied model, under the conditions cited above.

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