

# VALIDATION OF A DYNAMIC SYSTEM MODEL FOR THE COLON–RECTAL CANCER CELLS VIA CHEMICAL REACTION NETWORKS

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Each cell function is regulated by a complex signaling network that translates extracellular signals into cellular responses and whose alteration underline diseases as cancer [1].

From a mathematical perspective, this process can be modelled through a chemical reaction network (CRN) [2], i.e. through a graph whose nodes are the involved chemical species and the edges are the chemical reactions. By applying mass action kinetics, the concentration dynamics of the species in a CRN gives rise to a polynomial system of ordinary differential equations (ODEs).

Here we study and validate the CNR for the G0-G1-S transition of colon-rectal cancer cells presented by Tortolina and colleagues [3], involving 419 chemical species and 850 chemical reactions. In particular, we study the corresponding system of ODEs, by characterizing moiety conservation laws, asymptotic steady states, and numerical solutions. We then simulate the steady state of a physiological cell and quantify its alteration due to various combinations of loss and gain of function mutations. We validate our model by comparing our results with those in the literature on the effect of each mutation.

Our study represents the first step of a mathematical tool for the design of targeted drugs.

## References

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