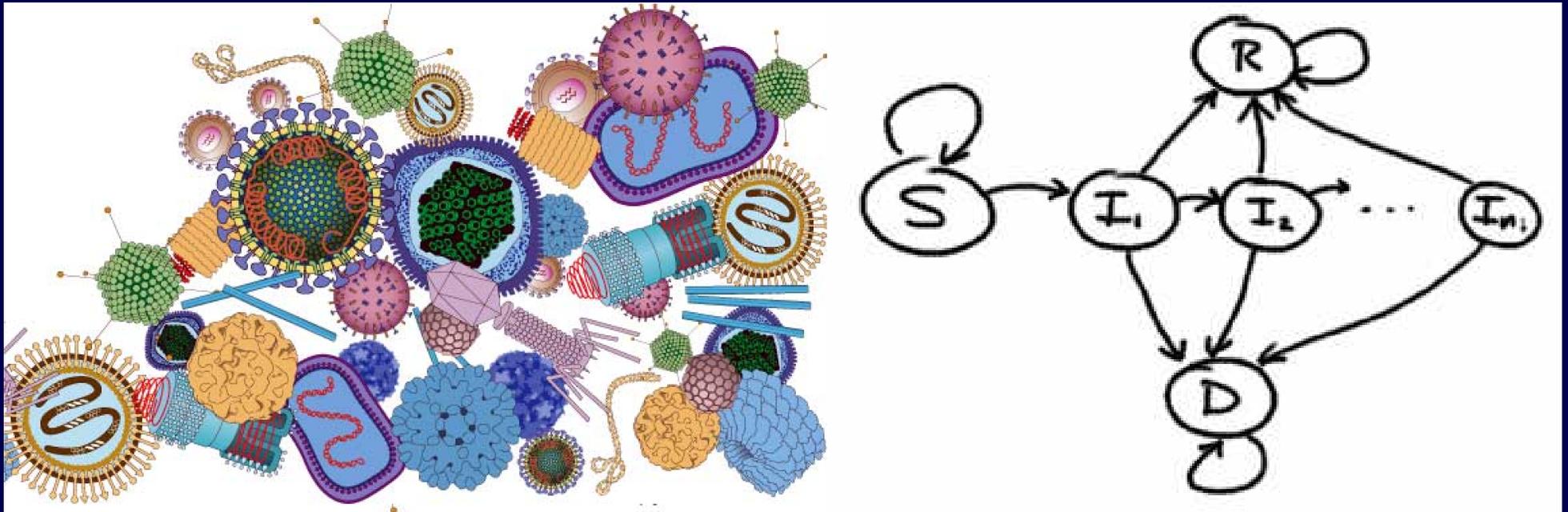


*On the origin of complex dynamics  
in multi-strain dengue models*

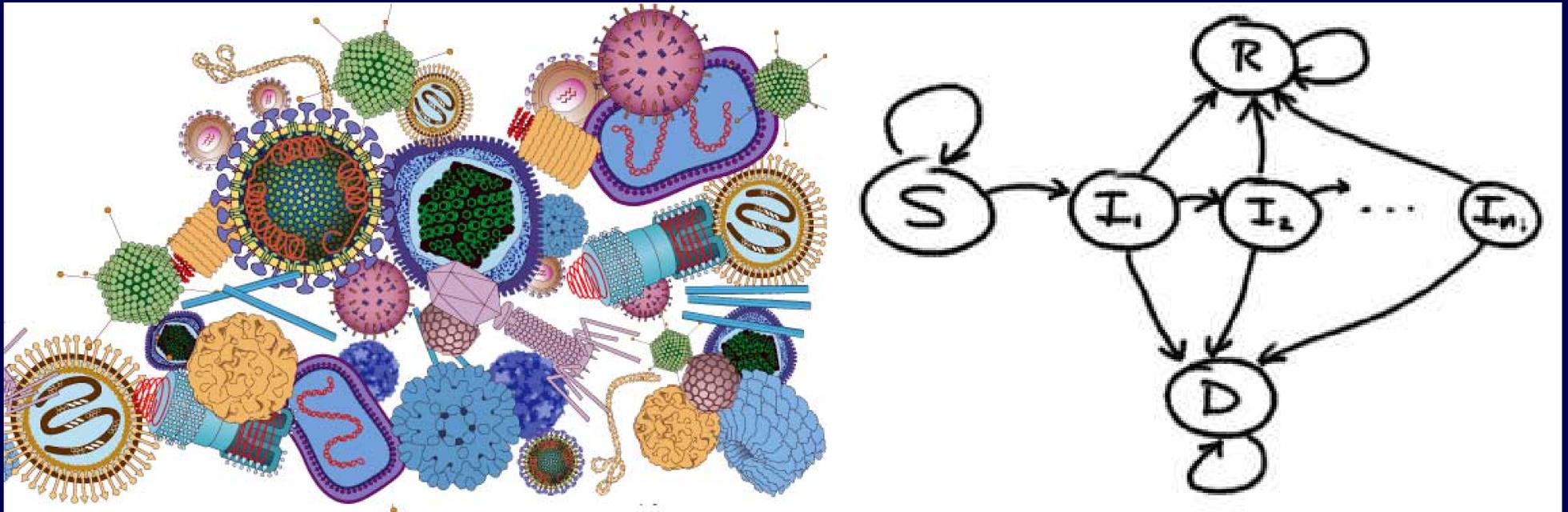


*Maíra Aguiar*

*Dipartimento di Matematica, UniTN, Italy*

*Basque Center of Applied Mathematics, BCAM, Spain*

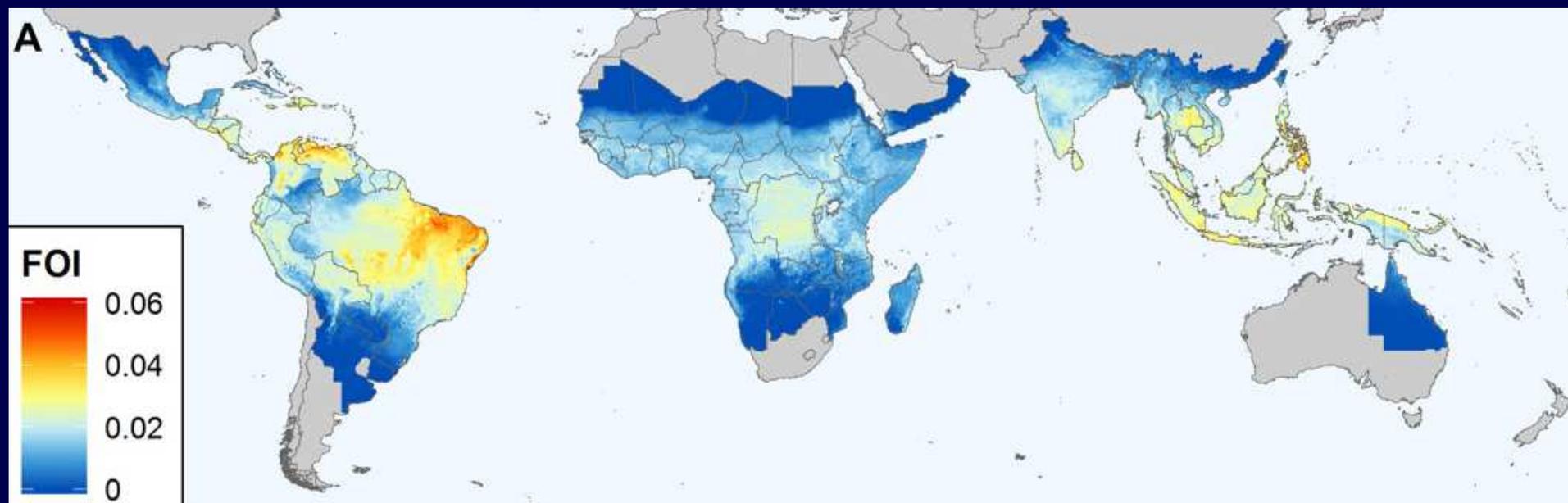
*On the origin of complex dynamics  
in multi-strain dengue models*



*... and its impact on public health interventions  
on chaotic epidemiological scenarios*

## *Dengue fever epidemiology and modeling assumptions*

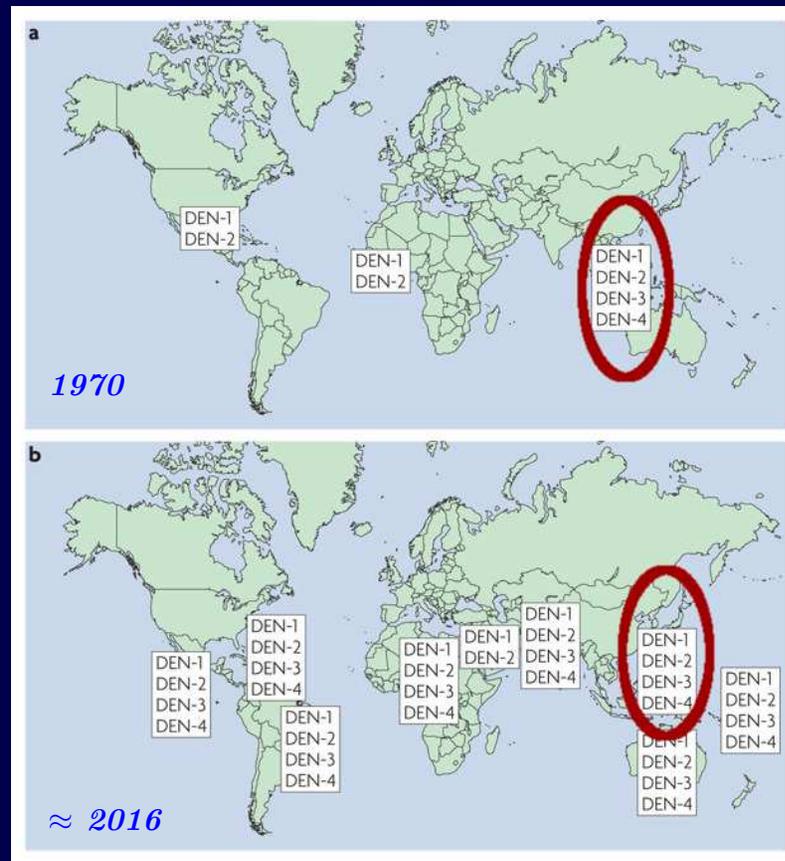
- \* Dengue is a viral mosquito-borne infection, a leading cause of illness and death in the tropics and subtropics.*
- \* More than one-third of the world's population are living in areas at risk of acquiring dengue infection.*



*Predicted global dengue risk (update to the estimates from Bhatt et al., Nature, 2013)*

*Lorenzo Cattarino et al., Science Translational Medicine, 2020*

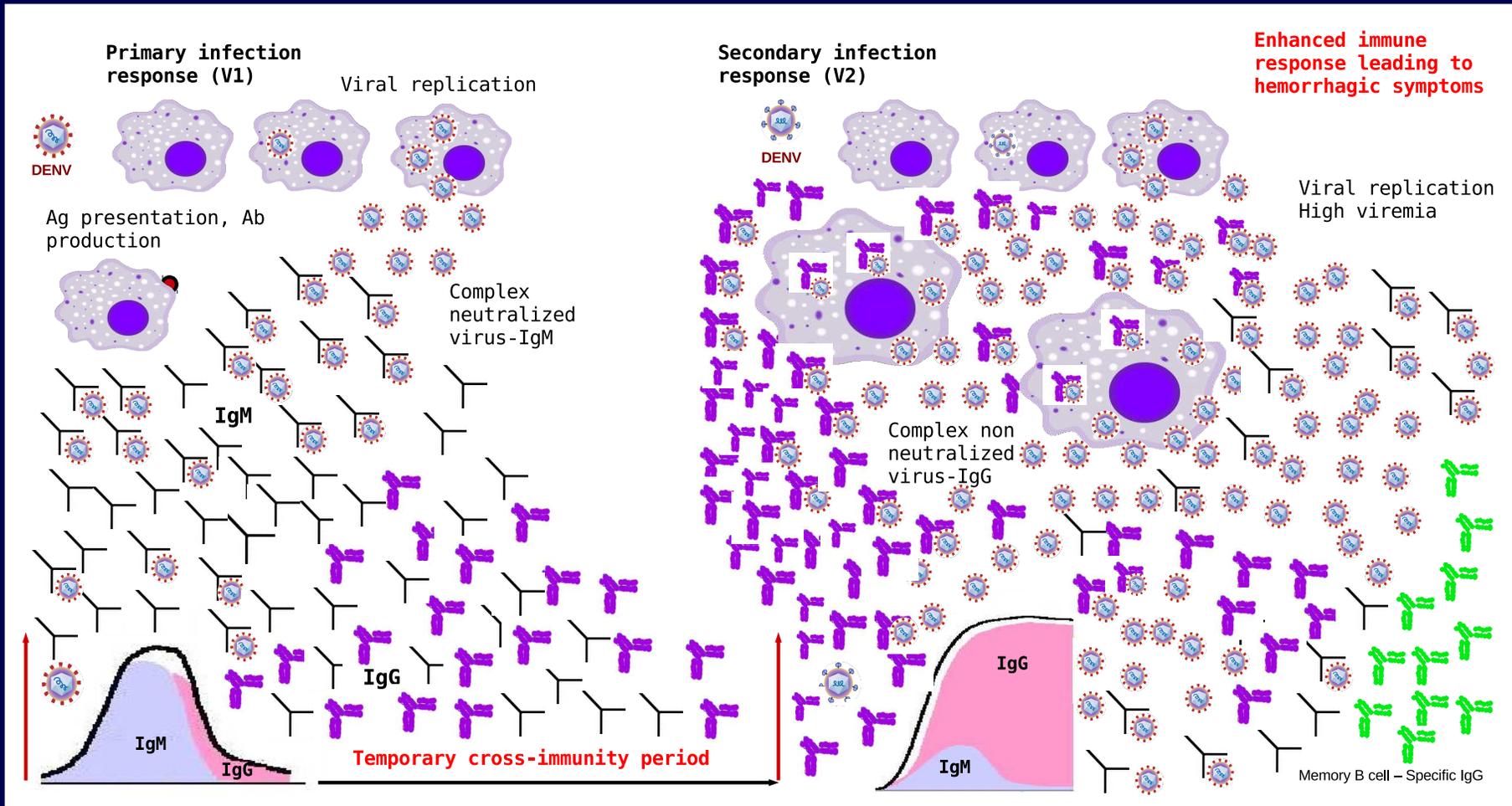
✧ *Four antigenically distinct but closely related dengue viruses: DEN-1, DEN-2, DEN-3, DEN-4.*



*Guzmán et al., Nat. Rev. Microbiol., 2010*

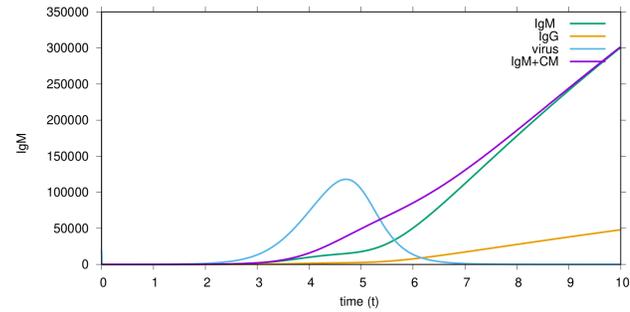
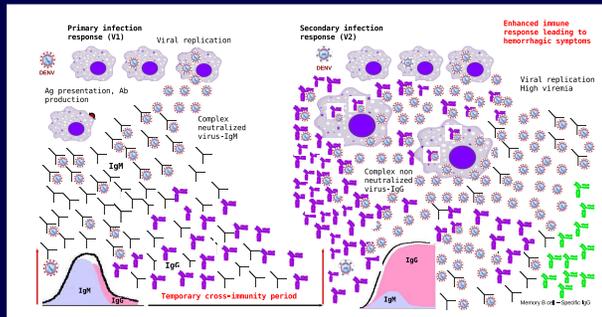
- \* Infection by one serotype confers life-long immunity to that serotype and a short period of temporary cross-immunity to other serotypes (3-9 months).*
- \* Dengue has a wide spectrum of clinical presentations: from asymptomatic to severe cases. Most patients recover following a self-limiting non-severe clinical course, a small proportion progress to severe disease, mostly characterized by plasma leakage with or without haemorrhage.*
- \* Epidemiological studies support the association of severe disease with secondary dengue infection, due to the antibody-dependent enhancement (ADE) process.*

# ADE in recurrent dengue infections for modeling purposes



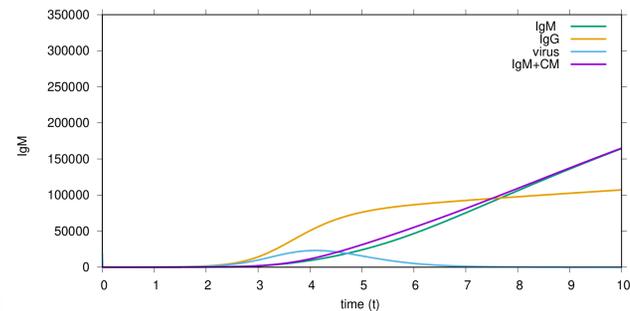
*Can we describe what happens  
within host using a simple model?*

# Modeling dengue immune responses mediated by antibodies



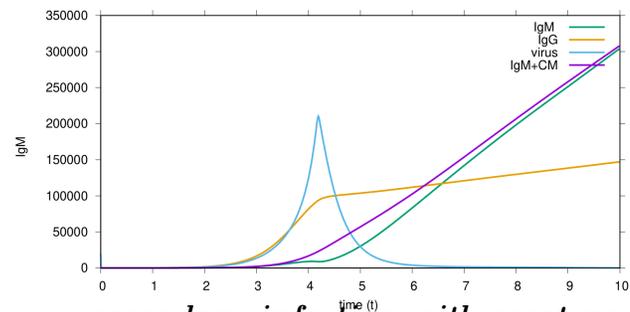
a)

*primary infection with serotype A*



b)

*secondary infection with serotype A*



c)

*secondary infection with serotype B*

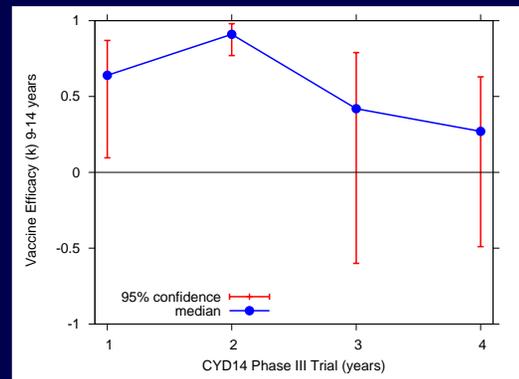
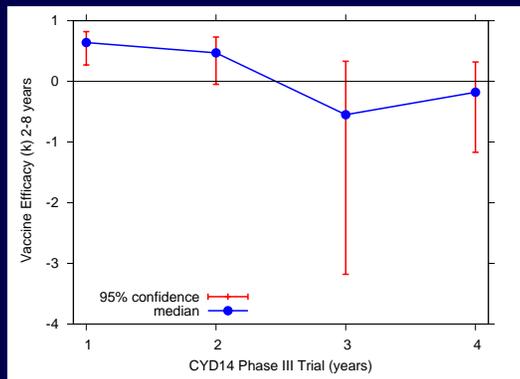
*Modeling insights are (but not restricted to)*

- \* Describe antibody depended-enhancement in a secondary dengue infection with a different virus.*
- \* Evaluate the role of temporary cross-immunity in the immunopathogenesis of severe disease.*
- \* Evaluate the impact of vaccination on disease prevention and control.*

*So far, we assume that...*

*In preparation with Edy Soewono*

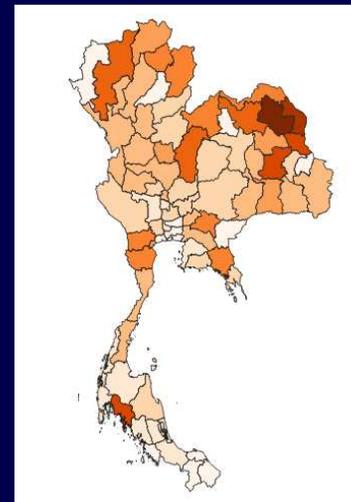
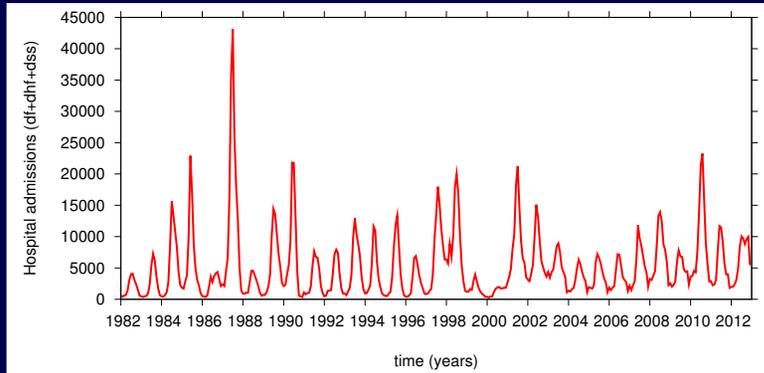
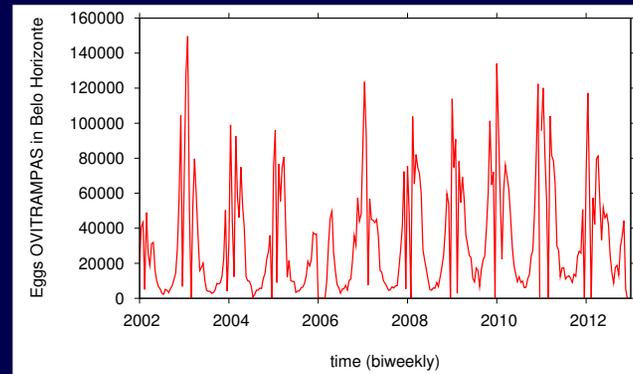
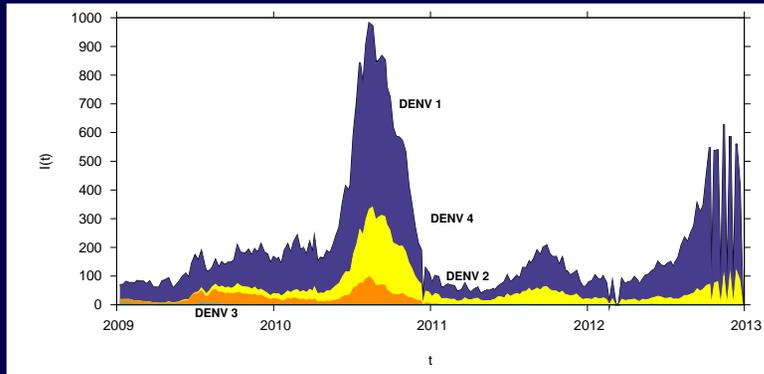
- ✧ *The majority of secondary dengue infections occur at a spacing of more than 6 month (seasonality + TCI).*
- ✧ *There is no specific treatment for dengue, and severe cases require hospitalization.*
- ✧ *The only licensed dengue vaccine, Dengvaxia, developed by Sanofi Pasteur had its Phase III trials successfully completed in the Asian-Pacific region and in Latin American countries.*



*vaccine efficacy estimation by age group*

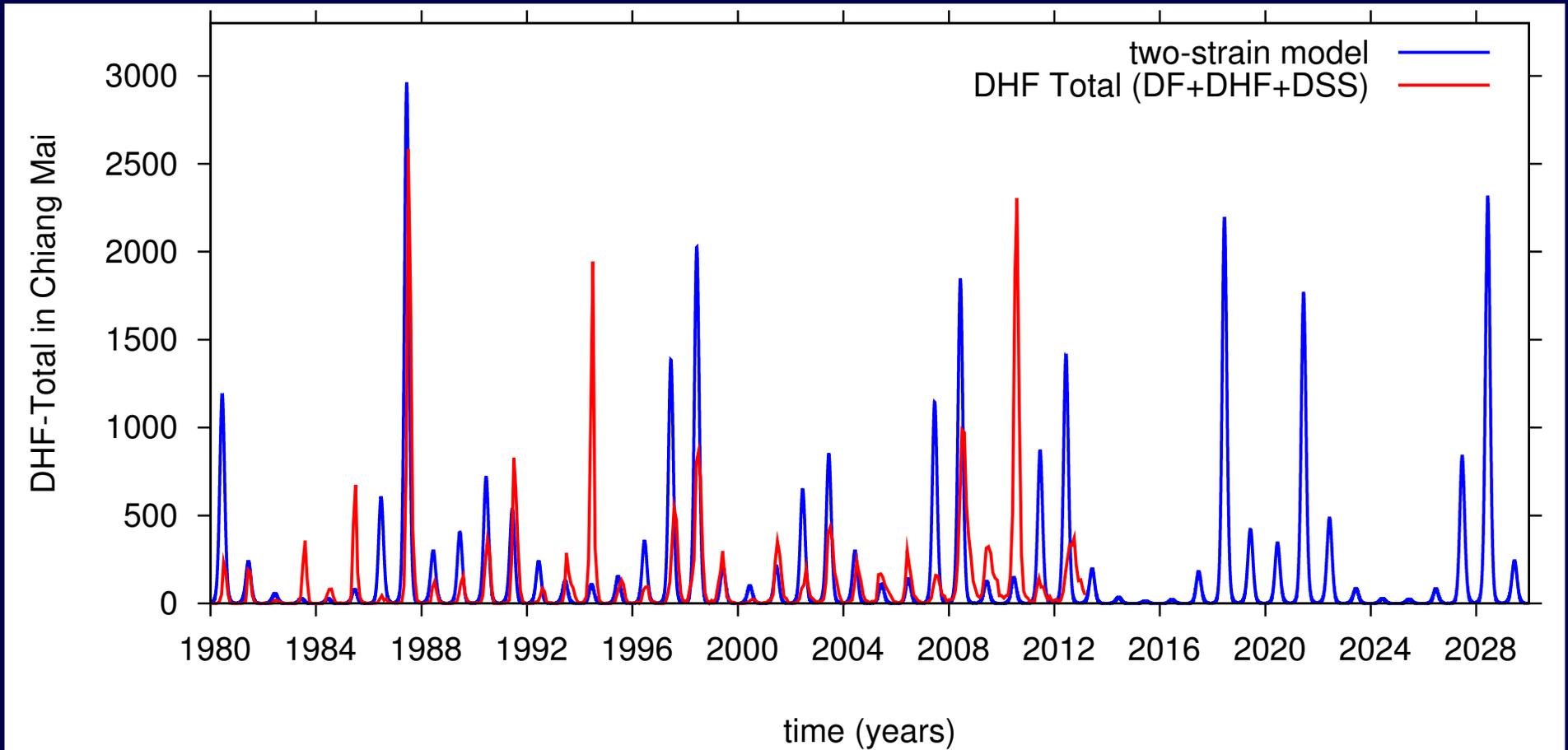
- ✧ *The much expected “primary findings” of the Takeda’s DENVax vaccine trial was recently published.*

## *Real world dengue data*



*define the model framework!*

## *Real world data matching*



*Source: Ministry of Public Health, Thailand. Bureau of Epidemiology.*

*How much complexity is needed?*

# *Modeling dengue fever epidemiology*

$\beta$  - *Infection rate*

$\phi$  - *Second. infection contribution*

*to the force of infection(ADE ratio)*

$\alpha$  - *Cross-immunity period*

$\gamma$  - *Recovery rate*

$\mu$  - *Demographic rate*

## *The n-strain epidemiological model*

$$\dot{S} = \mu(N - S) - \sum_{i=1}^n \frac{\beta}{N} S \left( I_i + \rho \cdot N + \phi \left( \sum_{j=1, j \neq i}^n I_{ji} \right) \right)$$

*and for  $i = 1, \dots, n$*

$$\dot{I}_i = \frac{\beta}{N} \left( I_i + \rho \cdot N + \phi \left( \sum_{j=1, j \neq i}^n I_{ji} \right) \right) - (\gamma + \mu) I_i$$

$$\dot{R}_i = \gamma I_i - (\alpha + \mu) R_i$$

$$\dot{S}_i = \alpha R_i - \sum_{j=1, j \neq i}^n \frac{\beta}{N} S_i \left( I_j + \rho \cdot N + \phi \left( \sum_{k=1, k \neq j}^n I_{kj} \right) \right) - \mu S_i$$

*and for  $i = 1, \dots, n$  and  $j = 1, \dots, n$  with  $j \neq i$*

$$\dot{I}_{ij} = \frac{\beta}{N} S_i \left( I_j + \rho \cdot N + \phi \left( \sum_{k=1, k \neq j}^n I_{kj} \right) \right) - (\gamma + \mu) I_{ij}$$

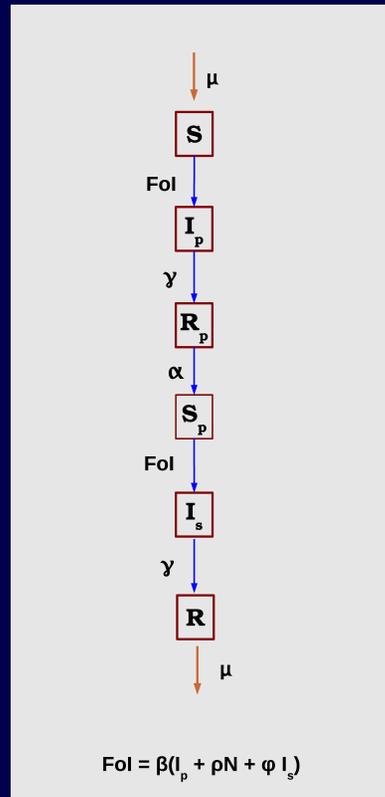
*and finally*

$$\dot{R} = \gamma \left( \sum_{i=1}^n \sum_{j=1, j \neq i}^n I_{ij} \right) - \mu R$$

*only two possible infections; low frequency of tertiary and quaternary infections*

*The 2-infections n-strain epidemiological  
model can be analyzed as follows*

## One-strain epidemiological, an Eq. system with 6 ODE's



$$\dot{S} = -\frac{\beta(t)}{N}S(I_P + \rho \cdot N + \phi I_S) + \mu(N - S)$$

$$\dot{I}_P = \frac{\beta(t)}{N}S(I_P + \rho \cdot N + \phi I_S) - (\gamma + \mu)I_P$$

$$\dot{R}_P = \gamma I_P - (\alpha + \mu)R_P$$

$$\dot{S}_P = -\frac{\beta(t)}{N}S_P(I_P + \rho \cdot N + \phi I_S) + R_P\alpha - S_P\mu$$

$$\dot{I}_S = \frac{\beta(t)}{N}S_P(I_P + \rho \cdot N + \phi I_S) - (\gamma + \mu)I_S$$

$$\dot{R} = \gamma I_S - \mu R$$

*No vector dynamics explicitly:  $\beta(t) = \beta_0(1 + \eta \cdot \cos(\omega t))$*

*Only two possible infections*

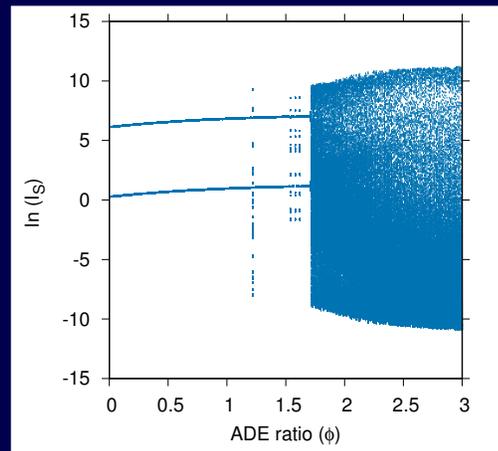
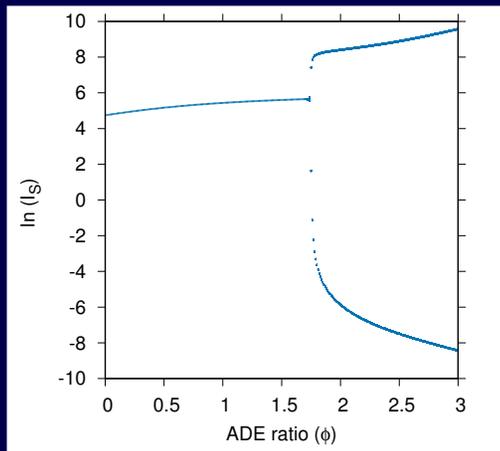
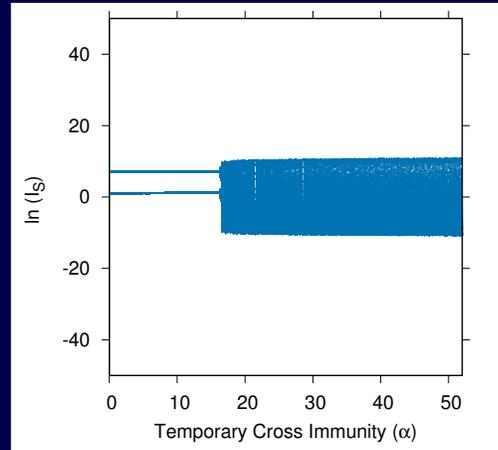
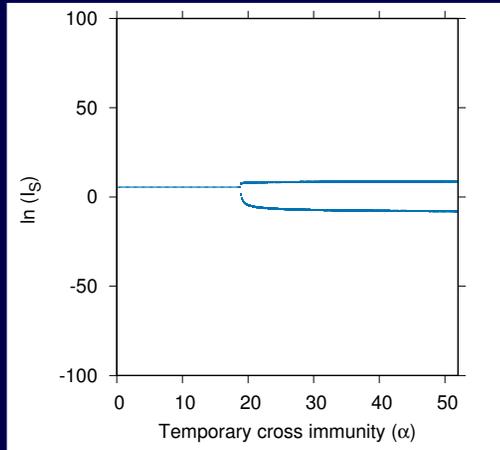
*(low frequency of tertiary and quaternary infections)*

# Bifurcation Diagram for ADE and TCI

*Non-seasonal*

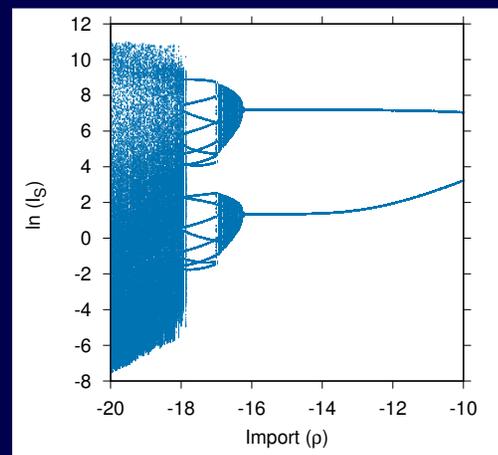
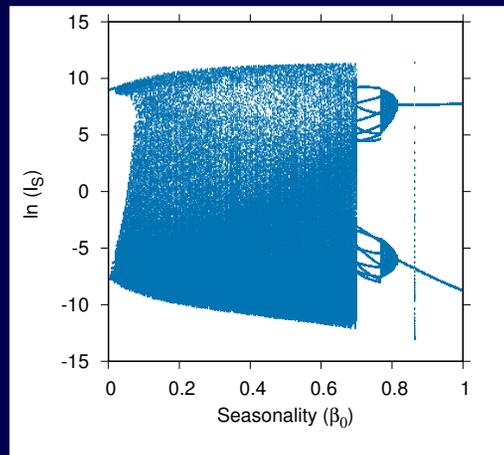
*Seasonal*

*Behaviour restricted to  $\alpha = 52$ ,  $\phi = 2.6$*

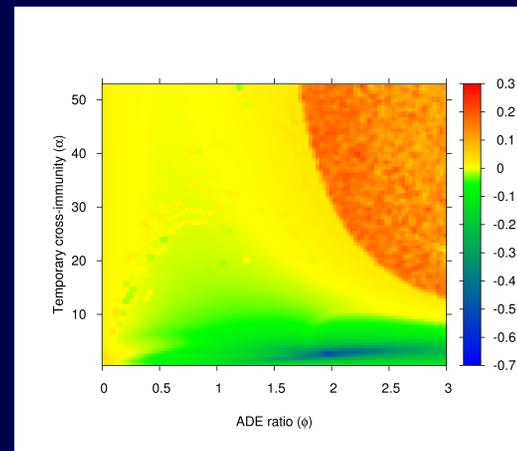
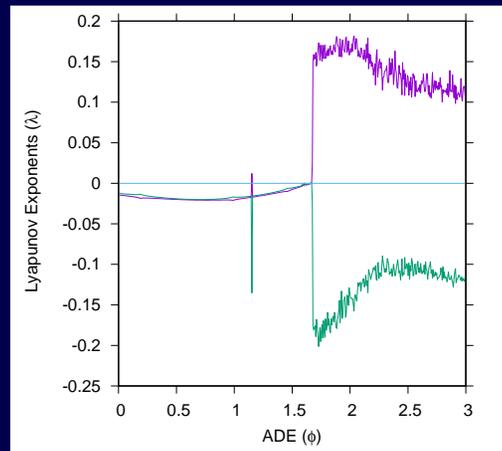


*Aguiar, M. Kooi, B.W, Stollenwerk, N and Pugliese, A. In preparation.*

## *Bifurcation Diagram for Seasonality and Import*

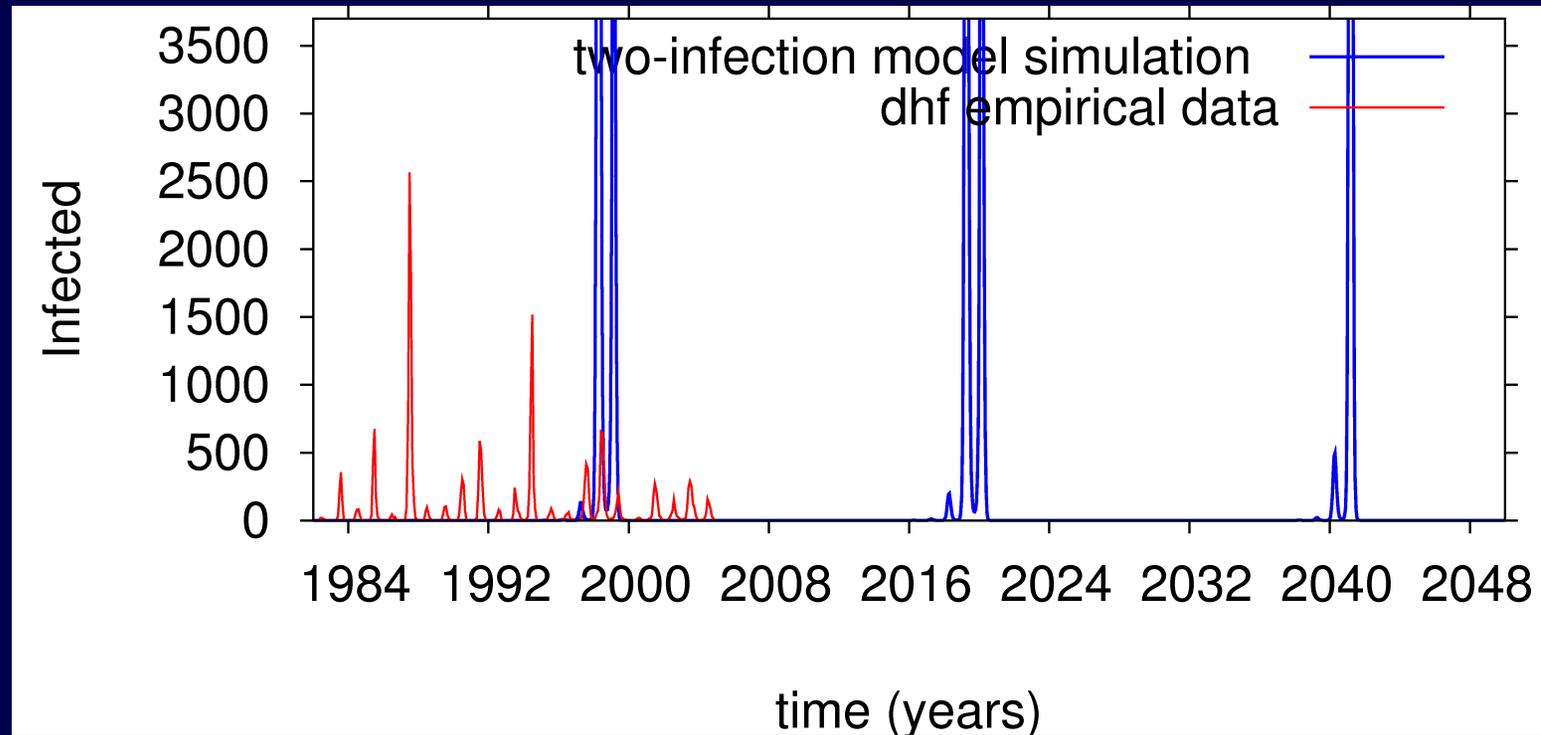


## *Lyapunov exponents and 2D Lyapunov spectra*



*$(\lambda_1 < 0)$  fixed point,  $(\lambda_1 = 0)$  limit cycle,  $(\lambda_1 > 0)$  chaos*

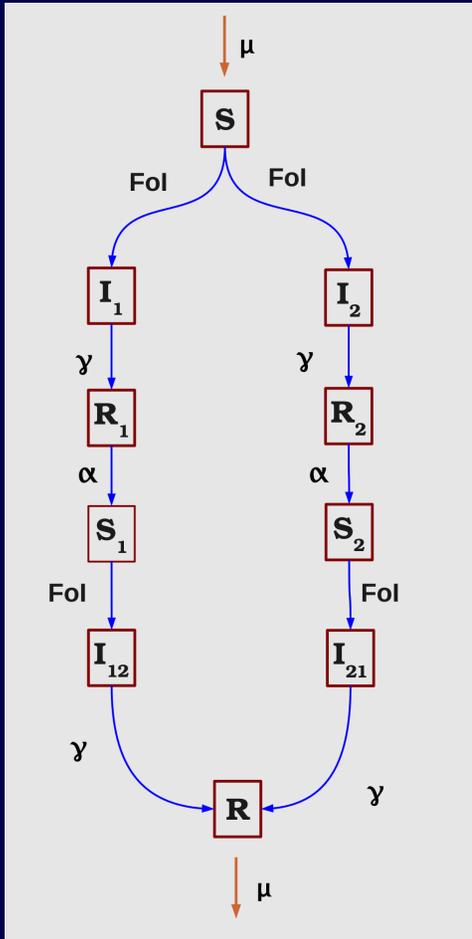
## *Time Series and Data Matching*



*Seasonal model:  $\alpha = 52$  and  $\phi = 2.6$*

*Irregular outbreaks every 25 years and not data alike*

## The 2-strain dengue model, JTB, 2011



$$\dot{S} = -\frac{\beta(t)}{N}S(I_1 + \rho \cdot N + \phi I_{21}) - \frac{\beta(t)}{N}S(I_2 + \rho \cdot N + \phi I_{12}) + \mu(N - S)$$

$$\dot{I}_1 = \frac{\beta(t)}{N}S(I_1 + \rho \cdot N + \phi I_{21}) - (\gamma + \mu)I_1$$

$$\dot{I}_2 = \frac{\beta(t)}{N}S(I_2 + \rho \cdot N + \phi I_{12}) - (\gamma + \mu)I_2$$

$$\dot{R}_1 = \gamma I_1 - (\alpha + \mu)R_1$$

$$\dot{R}_2 = \gamma I_2 - (\alpha + \mu)R_2$$

$$\dot{S}_1 = -\frac{\beta(t)}{N}S_1(I_2 + \rho \cdot N + \phi I_{12}) + \alpha R_1 - \mu S_1$$

$$\dot{S}_2 = -\frac{\beta(t)}{N}S_2(I_1 + \rho \cdot N + \phi I_{21}) + \alpha R_2 - \mu S_2$$

$$\dot{I}_{12} = \frac{\beta(t)}{N}S_1(I_2 + \rho \cdot N + \phi I_{12}) - (\gamma + \mu)I_{12}$$

$$\dot{I}_{21} = \frac{\beta(t)}{N}S_2(I_1 + \rho \cdot N + \phi I_{21}) - (\gamma + \mu)I_{21}$$

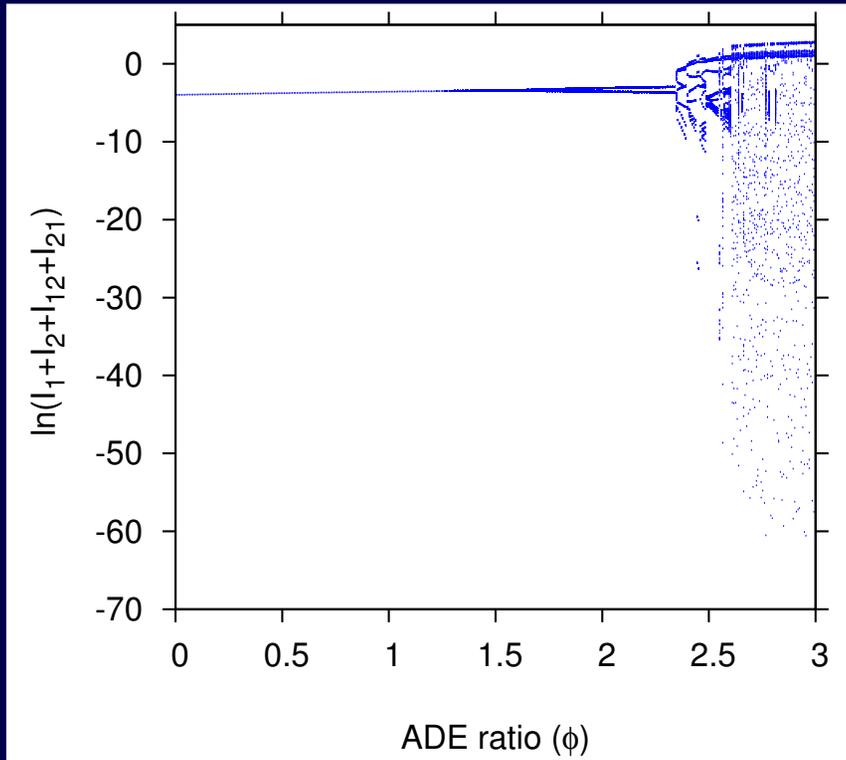
$$\dot{R} = \gamma(I_{12} + I_{21}) - \mu R$$

**No vector dynamics explicitly:**  $\beta(t) = \beta_0(1 + \eta \cdot \cos(\omega t))$

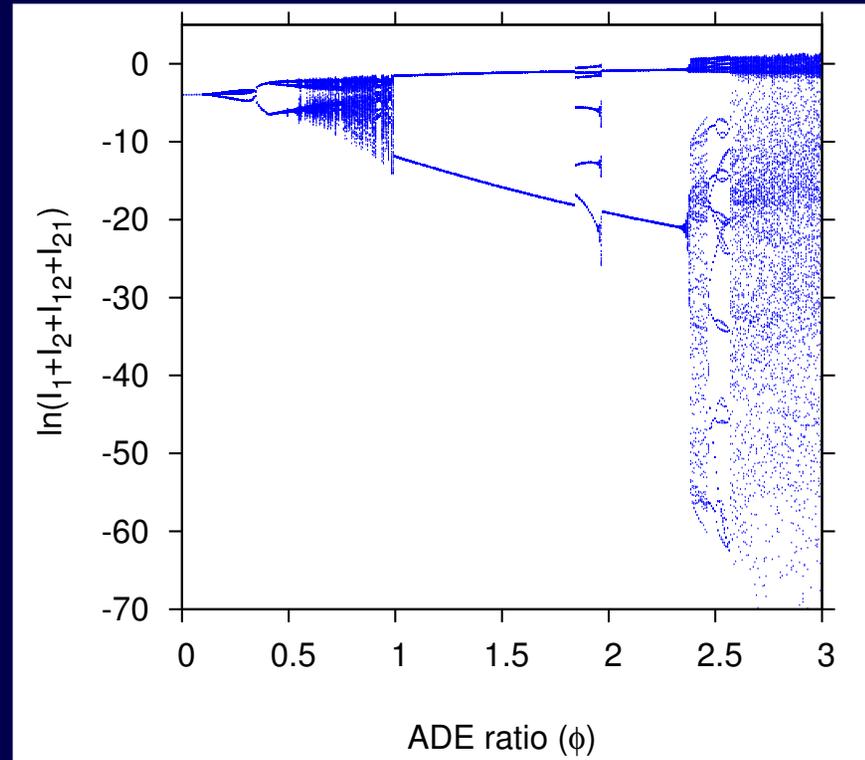
$FoI = \beta(I_1 + I_2 + \phi(I_{12} + I_{21}))$ . Only two possible infections.

(low frequency of tertiary and quaternary infections)

*Bifurcation Diagram for ADE (non-seasonal)*



$\alpha = 52$  (one week)



$\alpha = 2$  (six months)

*New chaotic window for  $\phi < 1$ !*

*More realistic due to hospitalization of the severe cases.*

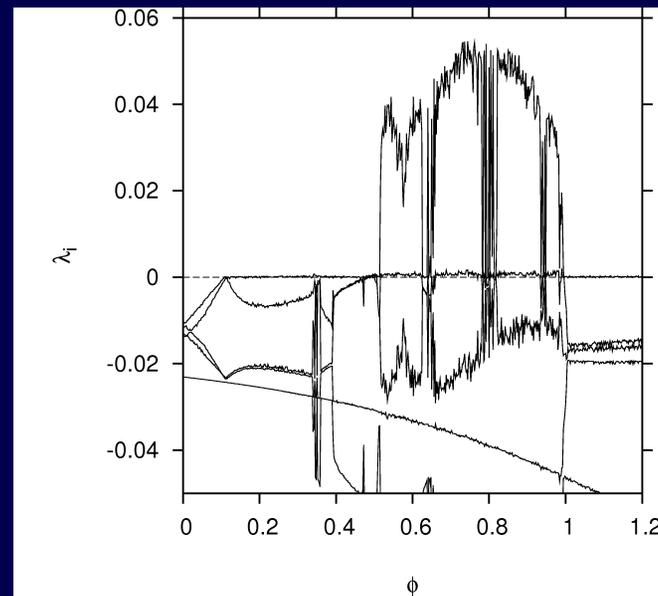
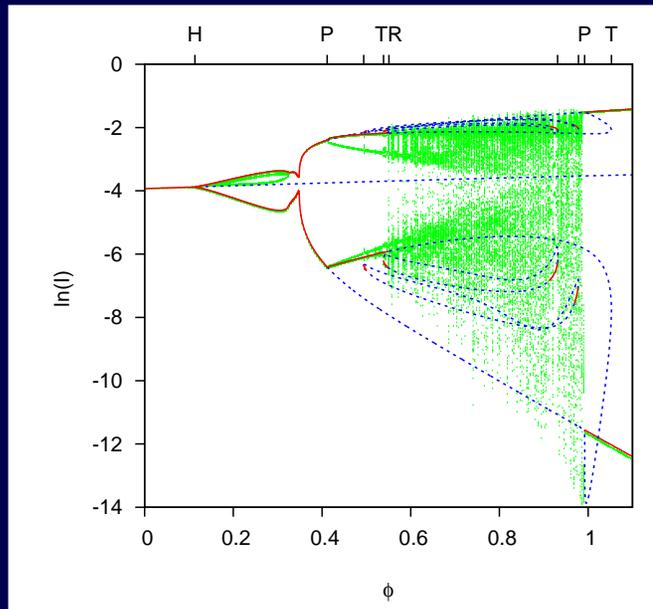
## Lyapunov exponents (non-seasonal)

$$\lambda_i = \frac{1}{n \cdot \Delta t} \ln \left( \prod_{\nu=0}^n |r_{ii}(\nu)| \right)$$

$\lambda < 0$  *fixed point*

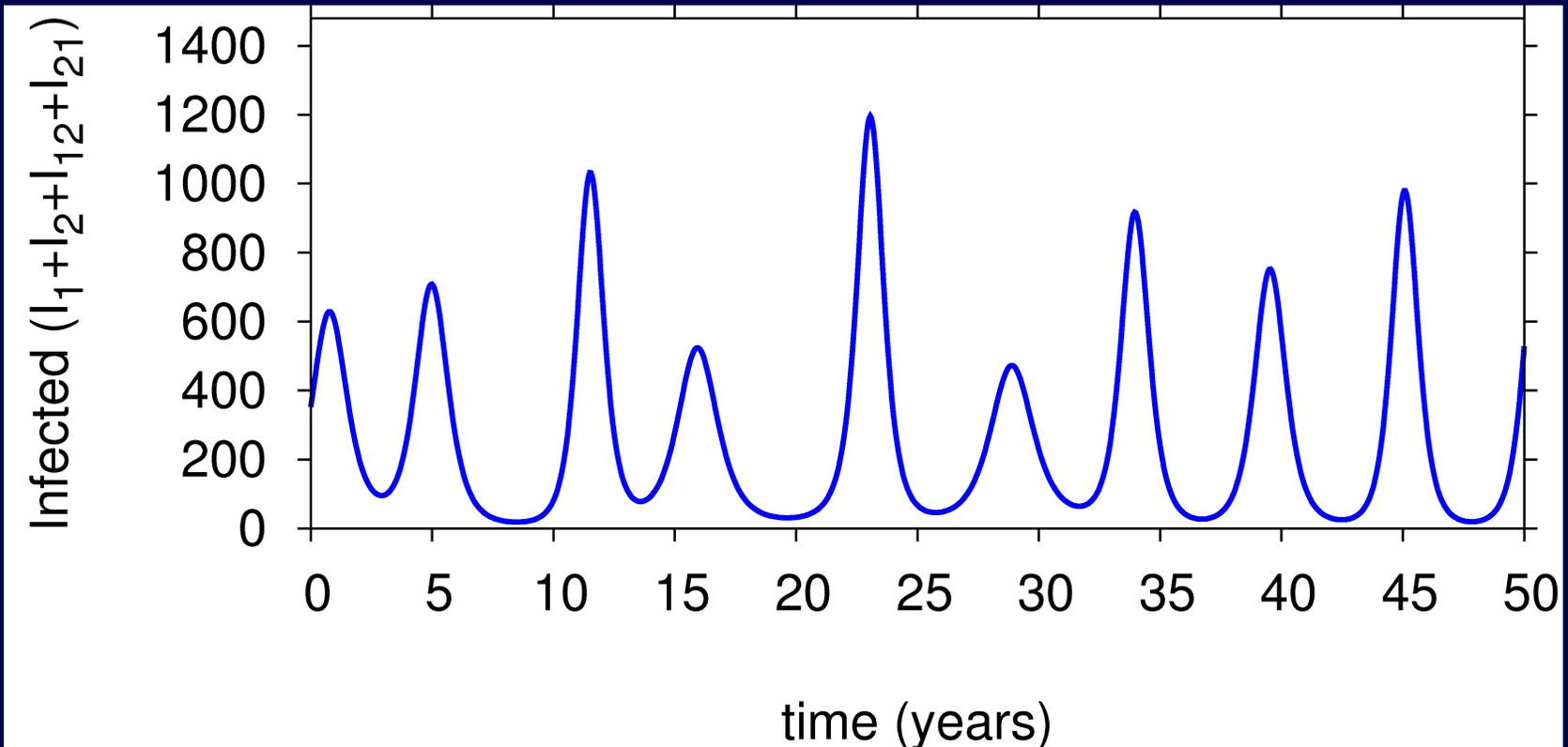
$\lambda = 0$  *limit cycle*

$\lambda > 0$  *chaos*



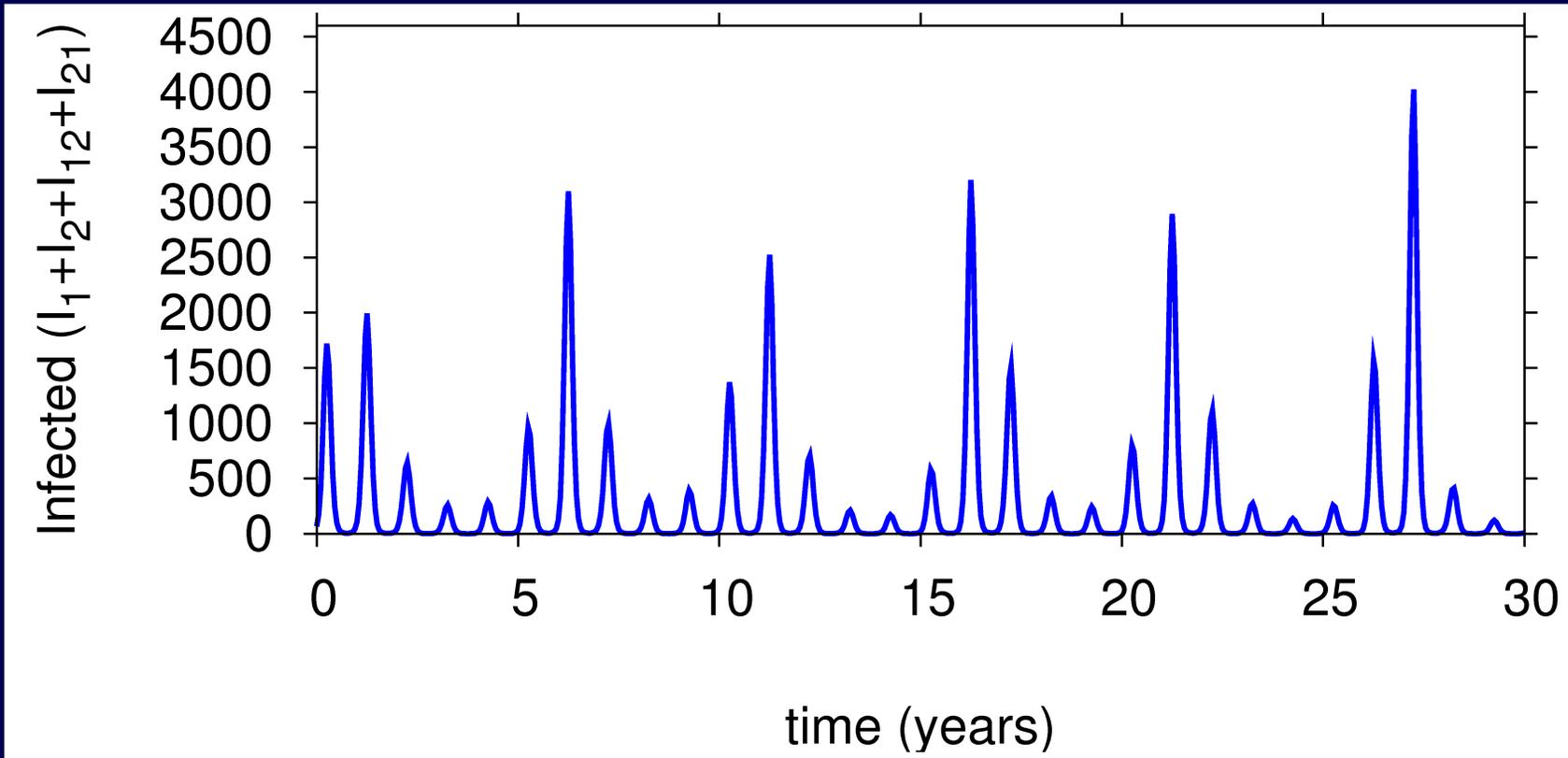
*Rich dynamic structure (Hopf, pitchfork, torus and tangent bifurcations) including deterministic chaos in a wider and more biologically realistic parameter regions ( $\phi < 1$ ), than previously expected.*

*Time Series (non-seasonal)*



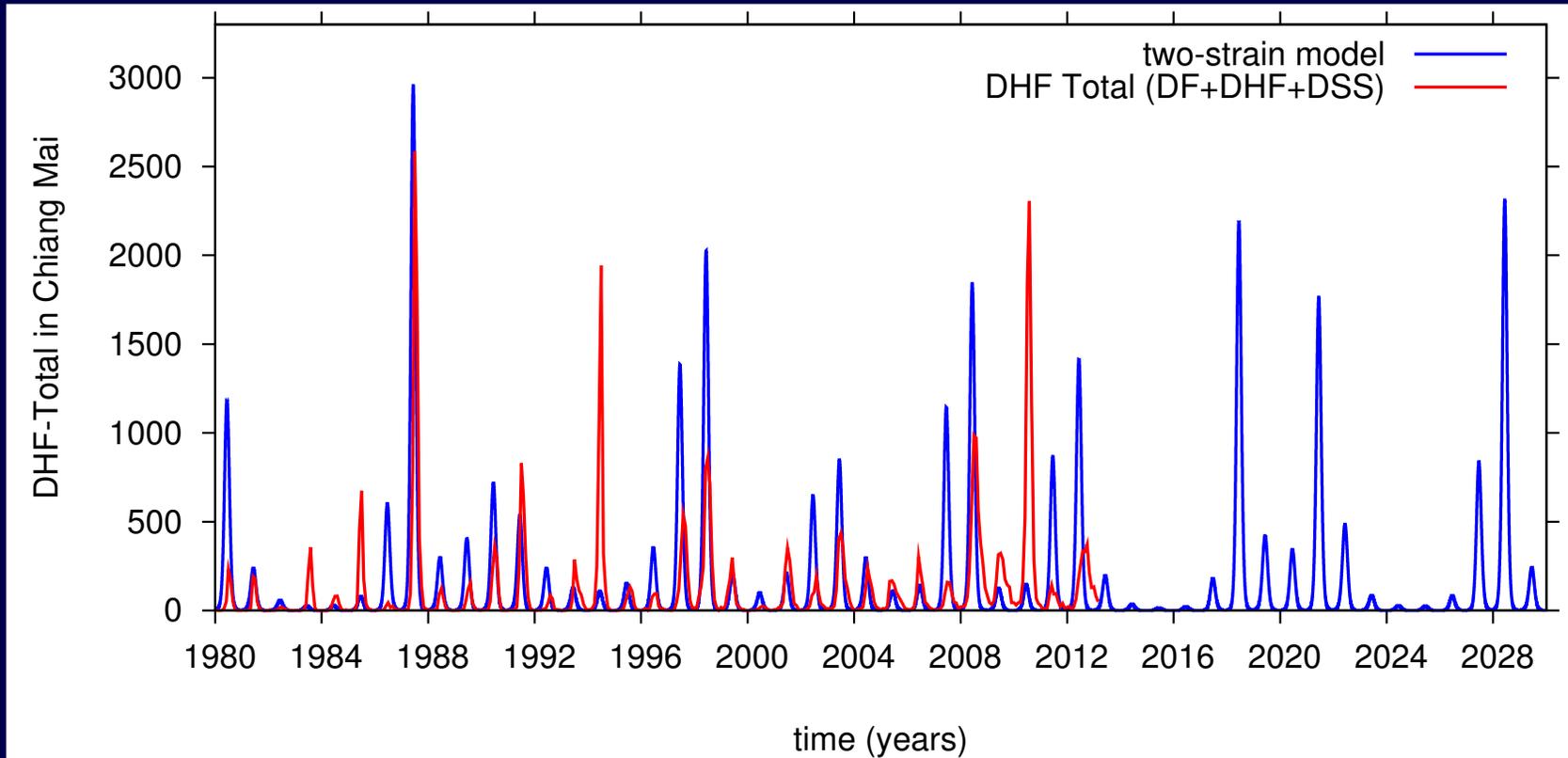
*Irregular pattern every 5 years.*

*Time Series (seasonal)*



*Realistic pattern with irregular, yearly and smooth outbreaks.*

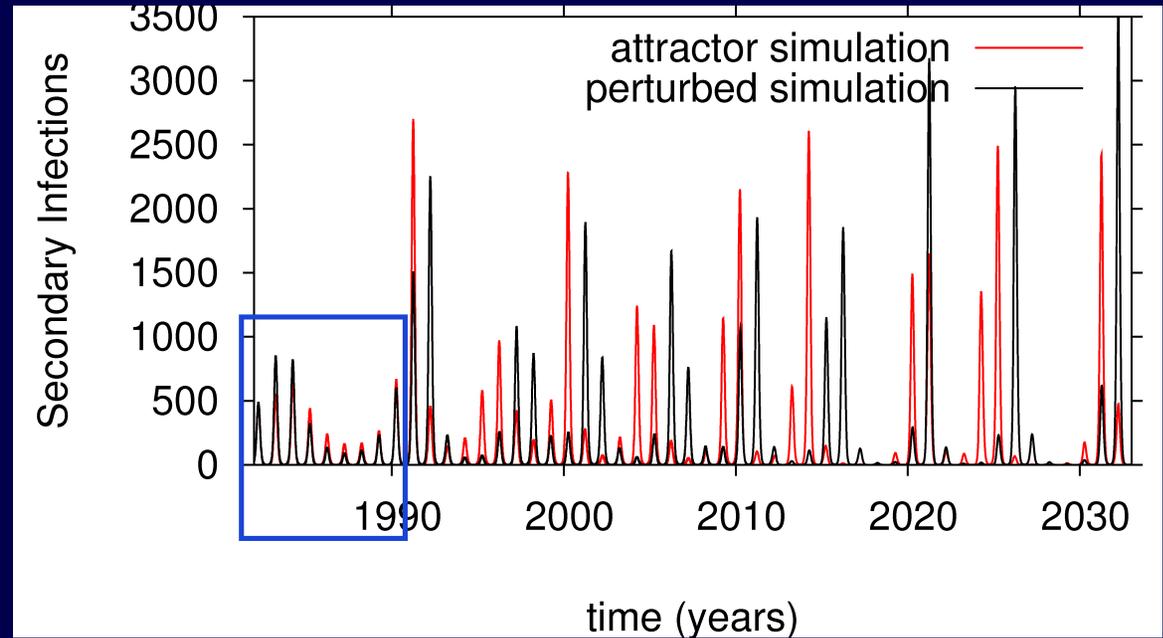
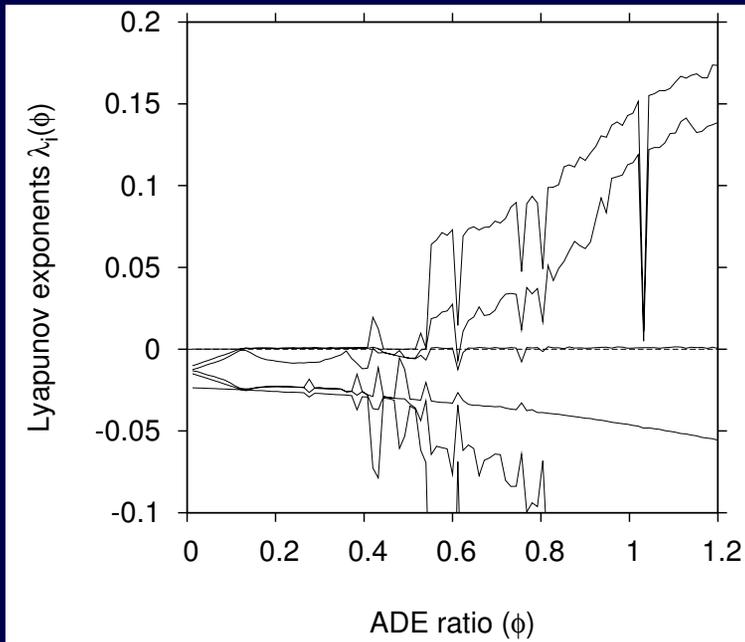
## *Time Series and Data Matching (seasonal)*



*Qualitatively a very good result when comparing empirical data and model simulation.*

*Aguiar et al. JTB, 2011*

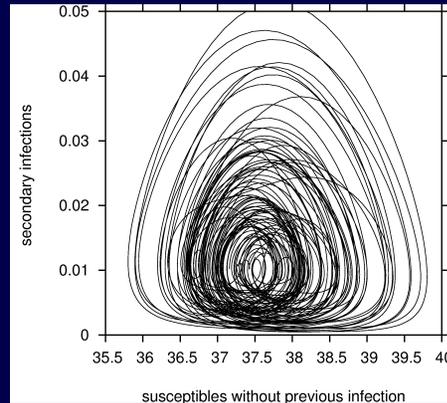
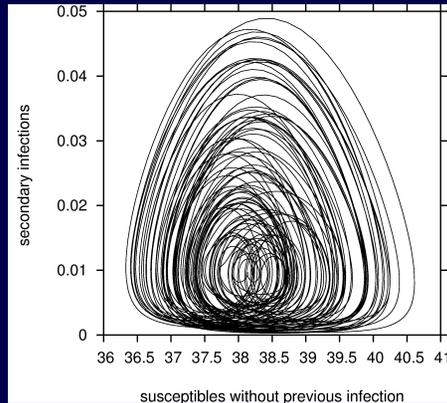
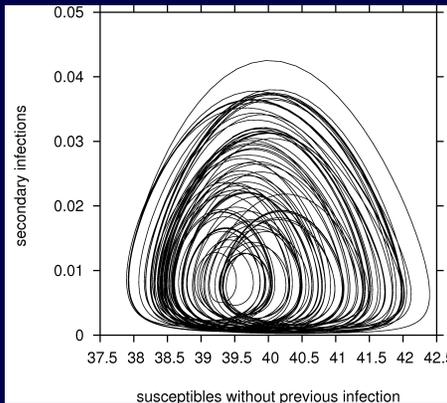
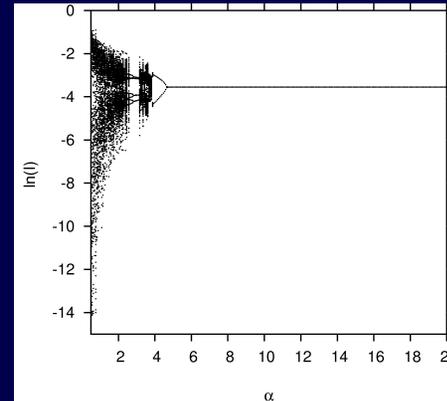
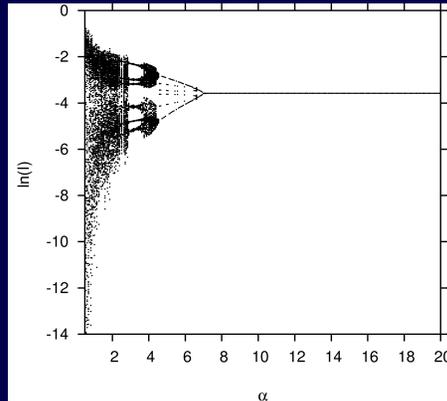
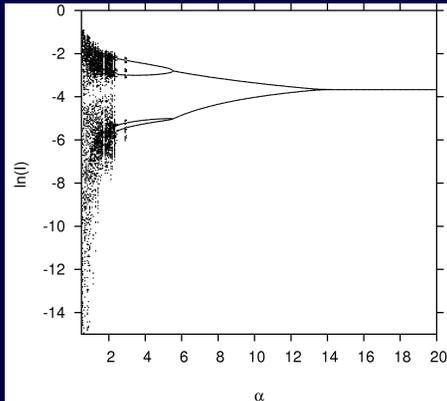
## *Lyapunov exponents and Average Predictability (seasonal)*



*Dominant Lyapunov Exponent (DLE) at  $\phi = 0.9$  is  $\lambda = 0.118$  giving  $\approx 8.5$  years of prediction horizon.*

*Aguiar et al. Ecol. Complex., 2013*

*Similarities between the 2-strain (10 ODE's),  
the 3-strain and the 4-strain (26 ODE's) dengue models*



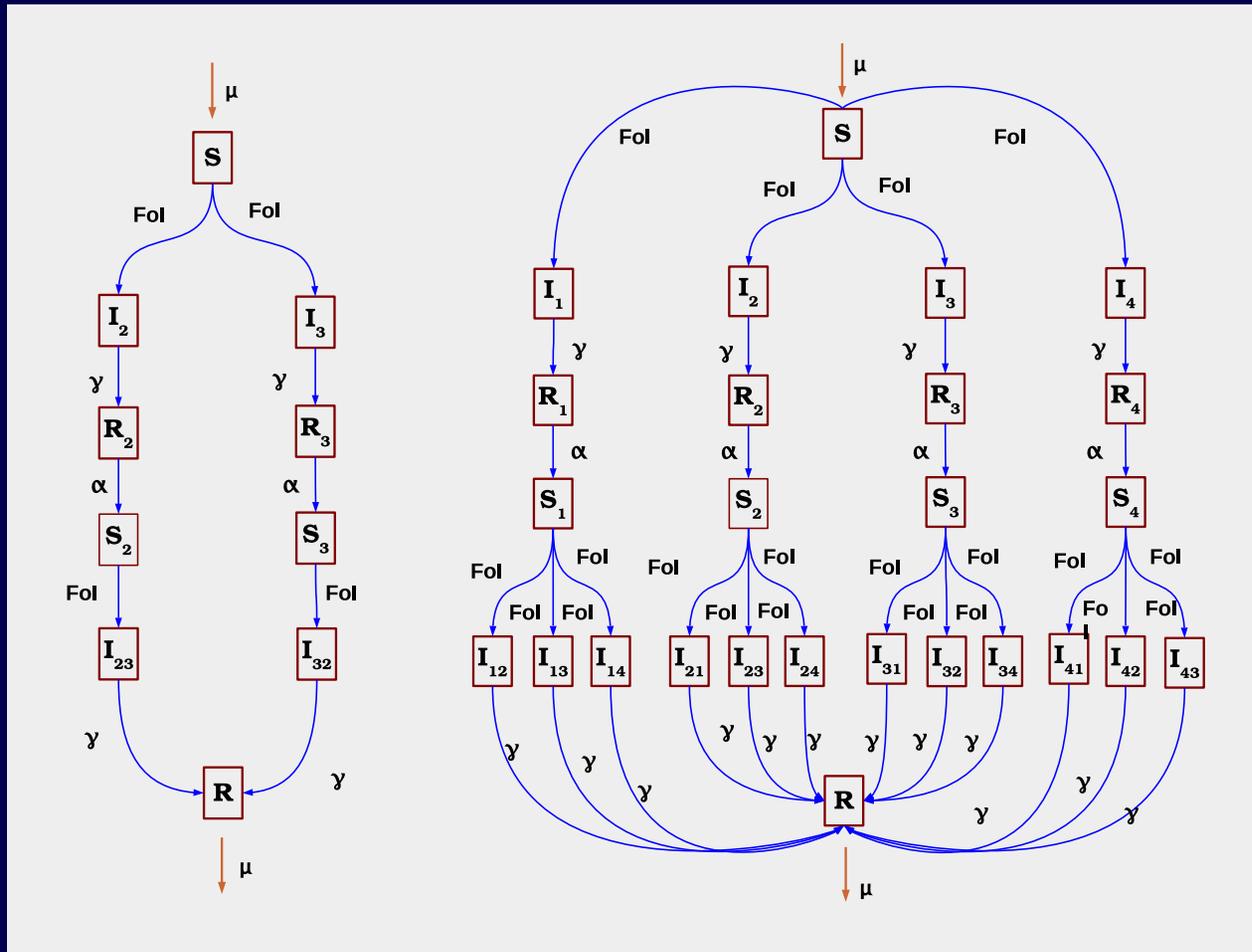
*2-strain model*

*3-strain model*

*4-strain model*

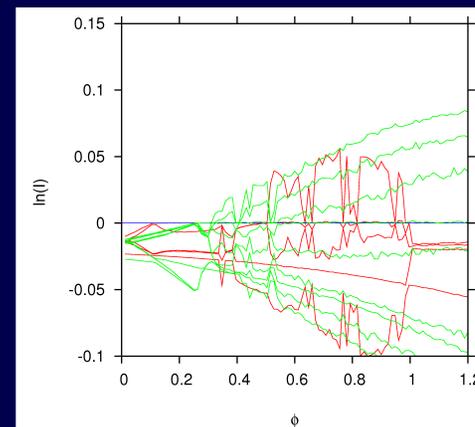
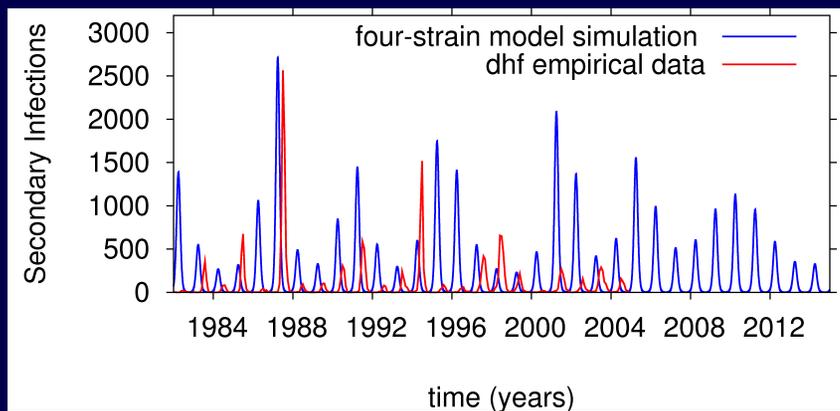
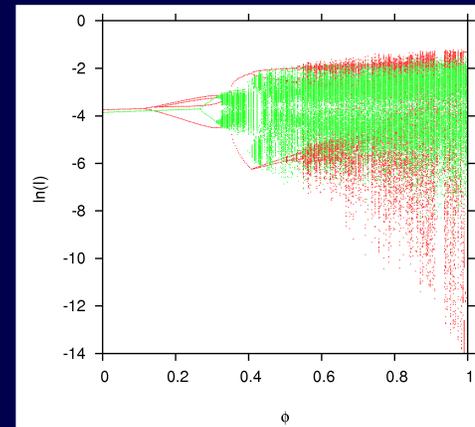
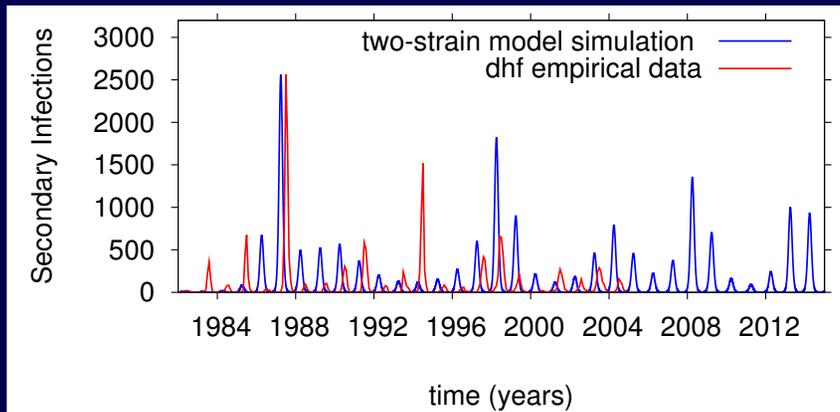
*Strain structure of pathogen shifts the chaotic behaviour to a more realistic parameter region (In preparation).*

## *Two-strain and four-strain epidemiological models: a dimensional problem*



*10 versus 25 dimensions!*

## *Two-strains (10 ODE's) and four-strains (26 ODE's)*



*Similar structure, order of magnitude  
and same prediction horizon (DLE).*

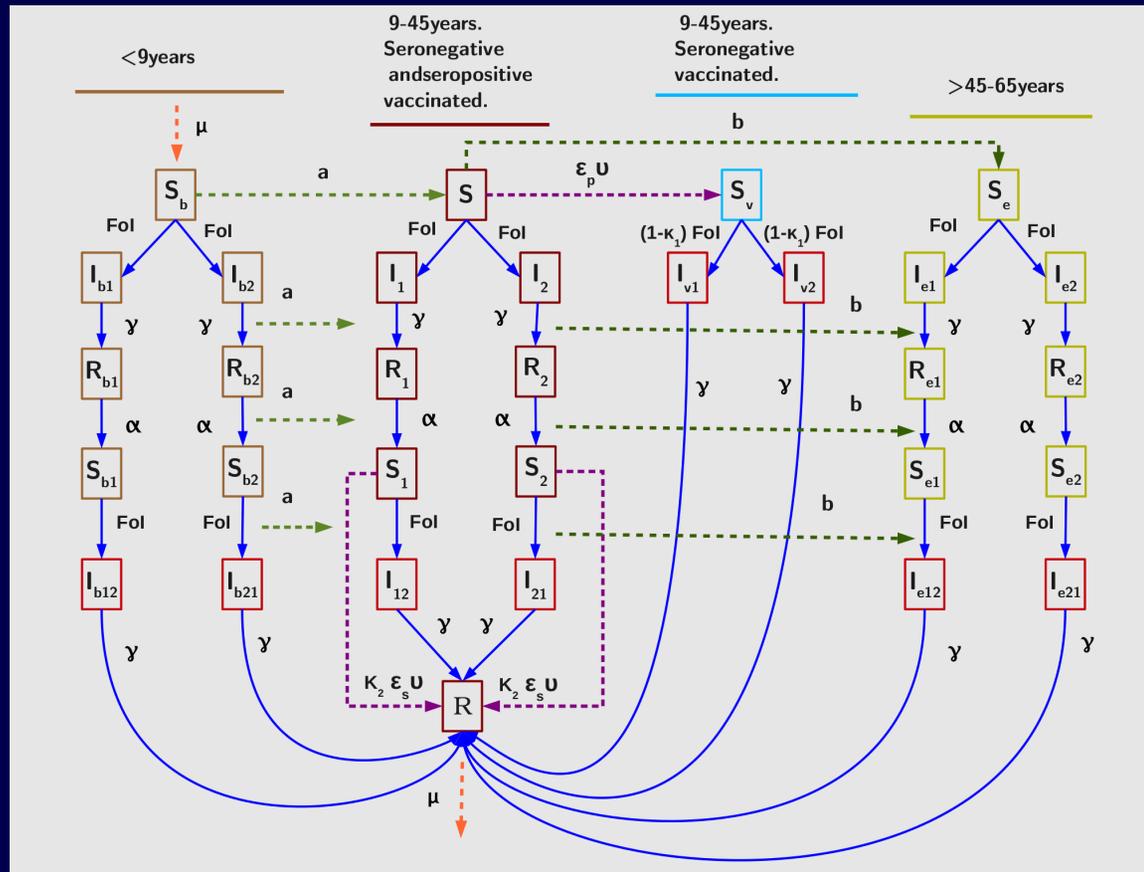
*2-strain chosen according to the parsimony law.*

*Aguiar et al. Ecol. Complex., 2013*

*Model extension to include vaccination*

# Modeling vaccine introduction phase

## Age-group-structured (2-strain) dengue model



5 years data matching — plus 5 years prediction

Aguiar, Stollenwerk and Halstead. PLoS NTDs, 2016

# Age-group-structured dengue model (extension of our pre-vaccination model)

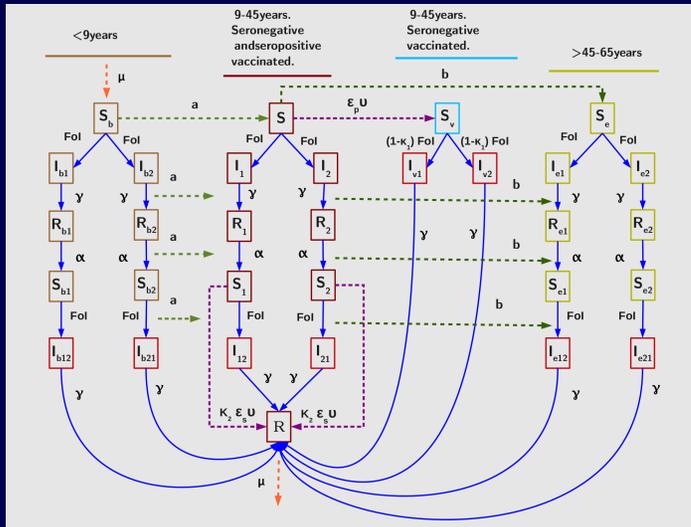
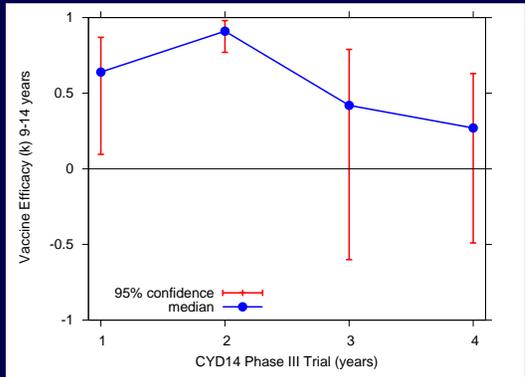
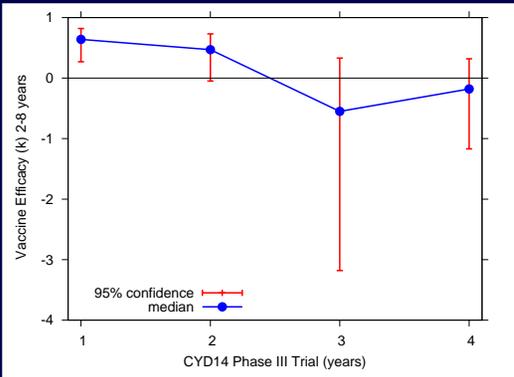
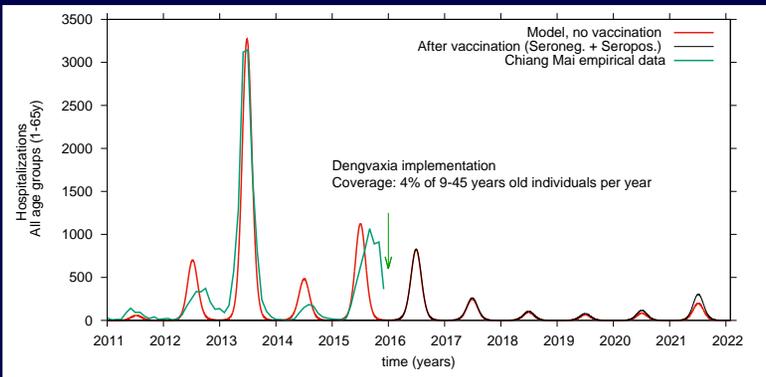


Table 8 Vaccine effect on hospitalized dengue of any severity (ITT population) over time for CYD14, CYD15, and CYD23/57. [32] and provided by manufacturer on request.

Age Group	Time Period	CYD14			CYD15			CYD23/57		
		CYD cases	Control cases	RR (95%CI)	CYD cases	Control cases	RR (95%CI)	CYD cases	Control cases	RR (95%CI)
2-5 Years CYD14 N=2451	Year 1 (Active)	8	6	0.644 (0.20-2.32)				1	2	0.239 (0.00-4.58)
	Year 2 (Active)	9	7	0.641 (0.21-2.02)			3	1	1.413 (0.11-74.17)	
	Year 3 (Hospital)	15	1	7.45 (1.15-313.80)			5	1	2.443 (0.27-115.54)	
	Year 4 (Hospital)	20	7	1.424 (0.58-3.99)	Not included in trial population			5	3	0.814 (0.16-5.24)
	Year 5 (Hospital/SEP)	6	2	1.495 (0.27-15.15)			4	0	∞ (0.32-∞)	
	Year 6 (Hospital)	NA	NA	NA			11	4	1.364 (0.40-5.76)	
Cumulative to date		58	23	1.256 (0.76-2.13)			29	11	1.274 (0.62-2.83)	
6-8 Years CYD14 N=2791	Year 1 (Active)	5	12	0.209 (0.06-0.64)			4	3	0.670 (0.11-4.57)	
	Year 2 (Active)	8	9	0.446 (0.15-1.3)			18	13	0.705 (0.33-1.57)	
	Year 3 (Hospital)	4	5	0.400 (0.08-1.86)			14	5	1.401 (0.48-4.97)	
	Year 4 (Hospital)	18	9	1.000 (0.43-2.53)	Not included in trial population			8	9	0.445 (0.15-1.30)
	Year 5 (Hospital/SEP)	5	3	0.833 (0.16-5.37)			3	1	1.498 (0.12-78.66)	
	Year 6 (Hospital)	NA	NA	NA			15	4	1.873 (0.60-7.75)	
Cumulative to date		40	37	0.541 (0.34-0.87)			62	35	0.890 (0.58-1.39)	
9-11 Years CYD14 N=2618	Year 1 (Active)	5	5	0.502 (0.12-2.18)	2	8	0.125 (0.01-0.63)	3	2	0.759 (0.09-0.08)
	Year 2 (Active)	2	13	0.077 (0.01-0.34)	6	14	0.214 (0.07-0.59)	3	9	0.169 (0.03-0.68)
	Year 3 (Hospital)	6	3	1.009 (0.22-6.23)	10	9	0.554 (0.20-1.54)	3	5	0.308 (0.05-1.58)
	Year 4 (Hospital)	12	3	2.013 (0.54-11.11)	6	5	0.601 (0.15-2.49)	3	5	0.308 (0.05-1.58)
	Year 5 (Hospital/SEP)	3	2	0.755 (0.09-9.04)	1	1	0.498 (0.01-39.12)	1	3	0.171 (0.00-2.13)
	Year 6 (Hospital)	NA	NA	NA	NA	NA	NA	11	5	1.126 (0.36-4.14)
Cumulative to date		28	26	0.542 (0.31-0.96)	25	37	0.337 (0.19-0.58)	24	29	0.422 (0.24-0.75)
12-16 Years CYD14 N=2309 (up to 14 yrs)	Year 1 (Active)	2	5	0.139 (0.02-1.22)	3	7	0.214 (0.04-0.94)			
	Year 2 (Active)	1	7	0.071 (0.00-0.55)	7	14	0.250 (0.09-0.66)			
	Year 3 (Hospital)	2	4	0.249 (0.02-1.74)	6	6	0.501 (0.13-1.87)			
	Year 4 (Hospital)	7	10	0.348 (0.11-1.01)	0	2	0.000 (0.00-2.67)			
	Year 5 (Hospital/SEP)	1	2	0.249 (0.00-4.79)	0	0	NC (NC)			
	Year 6 (Hospital)	NA	NA	NA	NA	NA	NA			
Cumulative to date		13	27	0.240 (0.11-0.48)	16	29	0.276 (0.14-0.52)			

N= denominator of evaluable subjects for the RR calculation for the entire study.  
SEP=Surveillance expansion phase.



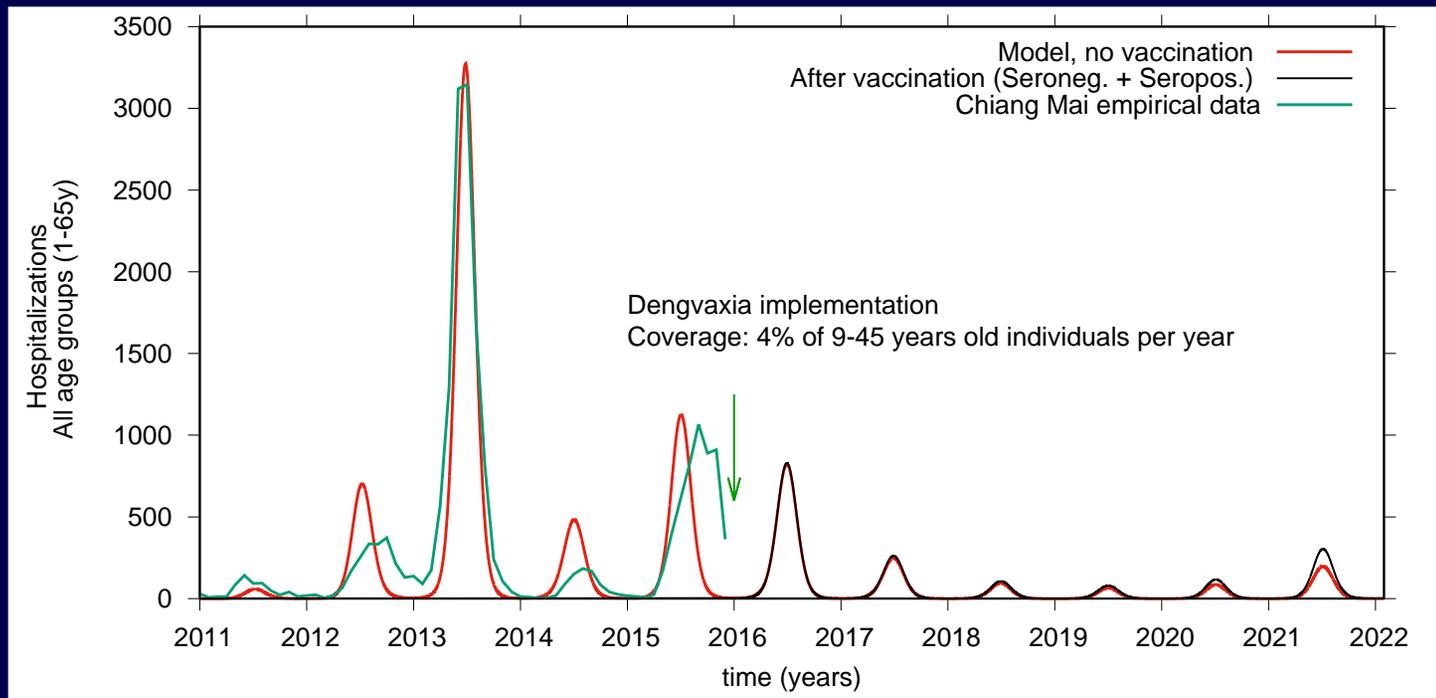
**NOT recommended for use in children under 9 years of age. Recommended for use in individuals 9-45 y, living in high endemic countries. During year 4, RR > 2 for age group 9-11 years!** Aguiar, Stollenwerk and Halstead, PLoS NTDs, 2016 & ERV, 2017

## *Modeling Dengvaxia introduction phase*

*Dengvaxia WITHOUT immunological screening*

*Vaccination coverage: 4% per year, seropos. and seroneg. individuals 9-45 years*

*All hospitalizations ( $\psi=1$ )*



*hospitalizations increase on average by 25% in 5 years*

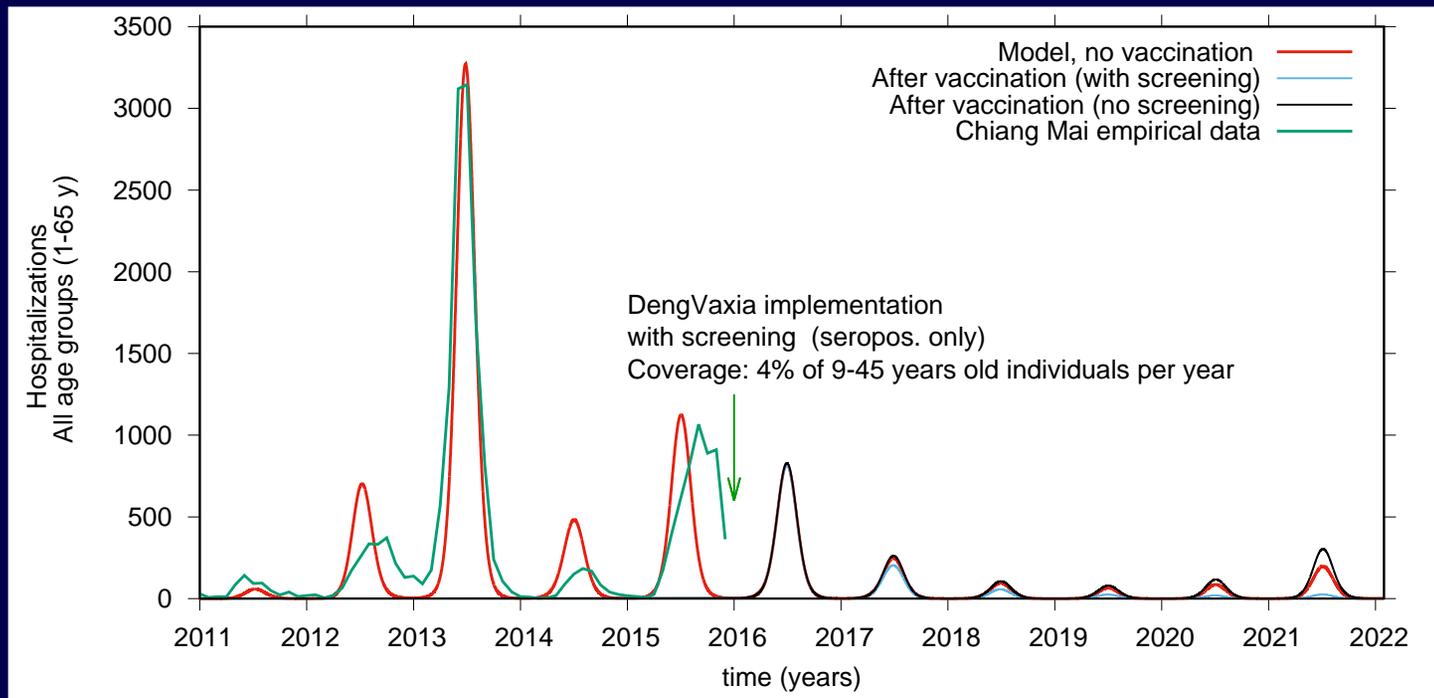
*Aguiar, Stollenwerk and Halstead. PLoS NTDs, 2016*

## *Modeling Dengvaxia introduction phase*

*Dengvaxia WITH prior immunological screening*

*Vaccination coverage: 4% per year, seropos. individuals 9-45 years*

*All hospitalizations ( $\psi=1$ )*

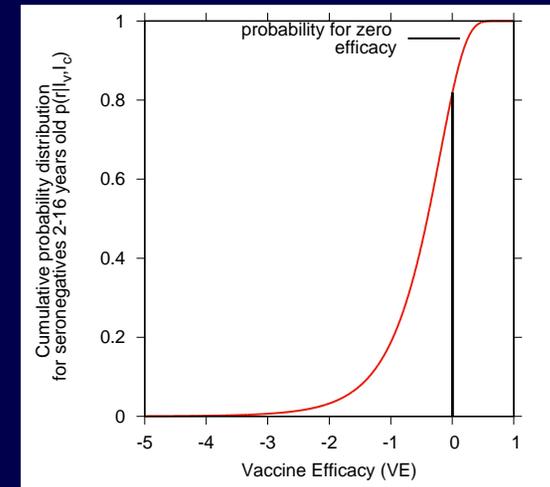
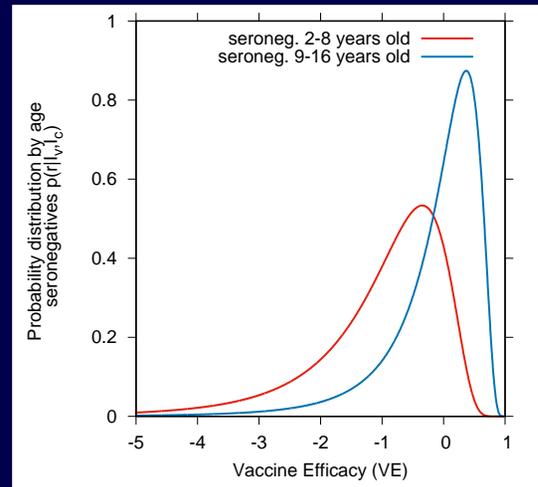
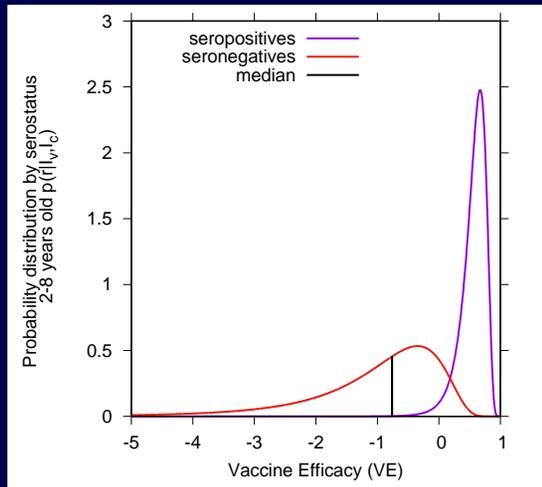


*overall reduction of hospitalization of more than 40% in 5 years.*

*Aguiar, Stollenwerk and Halstead. PLoS NTDs, 2016*

# Recent data and the concept of vaccine disease enhancement discussion

(Martinez-Vega et al., Vaccine, 2017)



Aguiar, M. & Stollenwerk, N., *Clinical Infectious Diseases*, 2017

*Individual serostatus is the most important feature when implementing this vaccine and that only individuals of any age who have experienced at least one dengue virus infection could benefit from vaccination.*

## *Dengvaxia, from 2016 to 2018*

- \* April 2016: recommended by the WHO, ignoring the observations (Phase III trial data) of high rate of hospitalizations in vaccinated seronegative children.*
- \* end of 2016-2017: implemented in two large vaccination programs, the Phillipines and Brazil, with more than 1 million children and adolescents vaccinated without any pre-vaccination testing.*
- \* end of 2017: Results from Sanofi's new test. Dengvaxia mass vaccination programs were suspended*
- \* mid of 2018: WHO new recommendation requiring a pre-testing before vaccination.*

*A bomb...*

*... that could have been avoided since 2 years earlier!*

**THE LANCET Infectious Diseases**  
Volume 16, Issue 8, August 2016, Pages 882-883

Comment  
**The risks behind Dengvaxia recommendation**  
Maira Aguiar <sup>a, b</sup>, Nico Stollenwerk <sup>a</sup>, Scott B Halstead <sup>c</sup>  
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Travel Medicine and Infectious Disease (2016) 14, 178–181  
Available online at [www.sciencedirect.com](http://www.sciencedirect.com)  
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Scott B. Halstead <sup>a, \*</sup>, Maira Aguiar <sup>b</sup>

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Maira Aguiar <sup>1, \*</sup>, Nico Stollenwerk <sup>1</sup>, Scott B. Halstead <sup>2</sup>

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Clinical Infectious Diseases, Volume 66, Issue 4, 1 February 2018, Pages 641-642,  
<https://doi.org/10.1093/cid/cix882>  
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EXPERT REVIEW OF VACCINES, 2016  
<http://dx.doi.org/10.1080/1476084.2017.1327631>

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Maira Aguiar <sup>a</sup>, Scott B. Halstead <sup>b</sup> and Nico Stollenwerk <sup>a</sup>  
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